The Tableau Workbench

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1 Introduction

Highly optimised provers like MSPASS [?] and FaCT [?] can test formulae with hundreds of symbols within a few seconds. Generic logical frameworks like Isabelle [?] allow us to implement almost any logical calculus as a “shallow embedding” with an automatic search tactic. But researchers often find these tools too complex to learn, program or modify. In the middle are the LWB [?], LoTReC [?] and LeanTAP [?] which implement many different logics or which allow users to create their own prover. The LWB provides a large (but fixed) number of logics while LoTReC requires the logic to have a binary relational semantics. These efforts to merge efficiency with generality highlight the mismatch between the high level concepts of the tableau method and the low level details of a generic implementation of it.

If you have just invented a new tableau calculus for a logic without such semantics, then LoTReC and the LWB are not very useful. Lazy logicians, as opposed to real programmers, usually then extend LeanTAP, but there is no generic LeanTAP implementation that contains features like loop-checking or further optimisations.

The Tableaux Work Bench (T WB) is a generic framework for building automated theorem provers for arbitrary (propositional) logics. A logic module defined by the user is translated by the T WB into OCaml code, which is compiled with the T WB

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libraries to produce a tableau prover for that logic. Lazy logicians can encode their rules easily to implement naive provers for their favourite logics without learning OCaml. Real programmers can use the numerous optimisation hooks to produce faster provers and even tailor the system to their own requirements by writing their own OCaml libraries.

Differences with previous version.

The TWB has been completely re-written since our system description in TABLEAUX 2003. Despite following the same design principles, we concentrated on simplifying the software both from the user and the developer points of view. The user interface has been completely changed to allow a more natural specification of logical rules. Ocaml code is no longer visible in the rule specification section, despite still being available to specify side conditions and functions. The architecture has also been substantially changed to increase modularity and to reduce code complexity. We also abstracted the core routine from the concrete data types and created a library to manipulate objects such as sets, multi-sets and lists in a generic way. In details these are the major changes:

- The user interface has been re-designed to allow a more natural specification of tableau/sequent rules. We removed the functional interface of the previous version of the TWB, where rules were defined as part of an Ocaml expression, and defined a new syntax. We also added the sequent interface.
- The connective section, in which the user could specify the concrete syntax of the connective used to define logical formulae has been replace by a new and more flexible way for defining the syntax via grammar definitions.
- The previous version of the TWB did not allow the user to define new data structures without re-compiling the TWB library. The new TWB now features a new abstract data type architecture that allows to re-use different components to create complex data structures at the user level.
- The core algorithm has been re-written and simplified. In the current version it is possible to specify multiple invertible rules and to chain rules in the strategy to compose different rules together.

2 Core Algorithm and Architecture

The core algorithm visits a tree generated by using a user-defined strategy to apply a finite collection of user-defined rules to an initial node containing a finite number of user-defined formulae. The TWB is organised into four main components which total roughly 4000 lines of OCaml code (loc). The core (∼ 400 loc) contains the visit algorithm, all type definitions and the strategy interpreter. The data-type library (∼ 700 loc) implements support data structures. The tableau library (∼ 800 loc) provides the machinery to implement tableau-based provers. The syntax library (∼ 1700 loc) allows a user to define specific logic modules. Finally the command line interface (∼ 250 loc) provides a way to compile and execute the logic modules on input formulae.
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\[
\begin{align*}
(\land) & \quad \frac{A \land B; Z}{A; B; Z} & (\land_{\text{inv}}) & \quad \frac{A \land B; X}{A; B; X} & (K) & \quad \frac{\Diamond P; \Box X; Z}{P; X}
\end{align*}
\]

Fig. 1. Definition of the (\land) and (\land_{\text{inv}}) and (K) rule.

3 Basic Notions

In this section we outline some well-known tableau principles which we used to specify logical rules in the TWB using a familiar notation. We will detail the TWB code in Section ??.

Tableau rules are of the form \( \frac{n}{d_1 \ldots d_m} \) where \( n \) is the numerator, while \( d_1 \ldots d_m \) is a list of denominators. The numerator contains one or more distinguished formula schemas called principal formulae and one or more formula schemas called side formulae. We use meta-variables \( A, B, P, Q, \cdots \) to represent principal formulae and \( X, Y, Z \) for, possibly empty, set of side formulae. Note that this notation is just for describing the theoretical rules clearly. As we shall see later, in the TWB, principal formulae are specified using an identifier in curly braces, while meta variables are specified using upper-case identifiers.

Operationally, tableau rules can be seen as functions to transform a node into a list of nodes during the construction of a graph. We say that a rule is applicable if we can partition the contents of the current node to instantiate the meta-variables in the numerator. The denominators of a rule represent actions to expand the graph by creating new nodes according to these instantiations.

The repeated application of rules gives rise to a tree of nodes, with children obtained from their parent by instantiating a rule. To capture sequent calculi as well as tableau calculi, we view this process as a search for a proof where all leaves are “closed”. But in general, for tableau calculi with cyclic proofs, there are really three notions: success, failure and undetermined: we stay with the dichotomy “closed” as success (of proof search) and “open” as failure (of proof search) for now to simplify the exposition.

A numerator pattern like \( Z \) is unrestricted since its shape does not restrict its contents in any way. Conversely, the pattern \( \Box X \) is restricted to contain only \( \Box \)-formulae, \( X \land Y \) is restricted to contain only \( \land \)-formulae while \( A \land B \) is restricted to contain exactly one single \( \land \)-formula. Patterns like \( X \land Y \) are allowed to be empty, but \( A \land B \) is not.

Figure 1 is seen as instructions to partition the contents of a node \( N \) to instantiate \( A \land B \) to a single \( \land \)-formula from \( N \) and to instantiate \( Z \) to all the other formulae so that \( Z = N - (A \land B) \) where “−” is the “subtraction” operator appropriate to our containers. In particular, if \( N \) is a set then there are no “hidden contractions”.

Similarly, the (K)-rule from Figure 1 instructs us to partition \( N \) into three disjoint parts: a single \( \Diamond \)-formula \( \Diamond P \); a container \( \Box X \) of \( \Box \)-formulae; and a container \( Z \) of all other formulae. The intended interpretation of the (K)-rule is invariably that \( Z \) should not contain any \( \Box \)-formulae since this ensures completeness of the rule. We therefore further assume that the partitions specified by the numerator are maximal.
Currently in the TWB, we forbid “purely structural” numerators like $X\cup Y$ which non-deterministically partition the node $N$ into two arbitrary disjoint containers $X$ and $Y$ (even though such numerators may be useful for linear logic), and numerators like $\Box X; \Box Y; Z$ since both can lead to an exponential number of possible different partitions.

3.1 Non-determinism

One of the main challenges when designing a generic tableau/sequent prover is to identify and to remove the non-determinism implicit in the pen-and-paper formulation of tableau systems. In general, we can identify three forms of non-determinism associated with three fundamental aspects of a generic tableau-based decision procedure:

**Node-choice**: the algorithm determines which leaf becomes the current node;

**Rule-choice**: the algorithm determines which rule to apply to the current node;

**Instance-choice**: a heuristic procedure determines the order in which to explore the different instantiations of the current node created by the chosen rule.

The first form of non-determinism is resolved in the TWB by using a depth-first visit function that deterministically selects the leftmost node as candidate. The second source of non-determinism is more complex and it arises from the lack of guidance when applying logical rules. For example, in classical propositional logic, where all rules are invertible, the order in which rules are applied is not important. However specifying a strategy that applies all linear rules and the axiom first, and then all branching rules, can potentially shorten the proof tree. The problem is however different in basic modal logic, where not all sequences of rule applications ensure a solution since the $(K)$-rule is not invertible. That is, the linear $(K)$-rule shown contains some “implicit branching” since we may need to backtrack over the different choices of principal formulae until we find a closed branch.

The problem is even more complicated in tableau-sequent calculi with more than one non-invertible rule: for example intuitionistic logic as in [?]. In this situation, at any given choice point, after all invertible rules are applied, we are forced to guess which non-invertible rule to apply, and eventually to undo this decision if it does not lead to the construction of an acceptable proof tree. Consequently, if the proof tree obtained from the application of the first rule of a sequence of non-invertible rules does not respect a logic-specific condition, the entire proof tree generated from that rule application must be discarded. To recover from this wrong choice, the proof must be re-started using the next non-invertible rule available in the sequence.

In the TWB we address all these issues by coupling tableau rules with a *strategy* to control the order in which rules are applied. In particular the strategy we employ uses the following operators given current node $N$:

- **Basic tactic**: the basic tactic is a rule and it is identified by a rule name (e.g. Id). A rule succeeds if it is applicable;
- **The strategies Skip and Fail** are two basic strategies that respectively, always succeed or always fail. The strategy *Skip* is the same as writing a rule that is always applicable and does nothing. The strategy *Fail* is the same as writing a
rule that is never applicable.

- Deterministic alternation, written as $t_1!t_2$, is the strategy that behaves as $t_1$ if the first rule of $t_1$ is applicable otherwise behaves as $t_2$. If the strategy $t_1$ is selected, the operator $!$ does not backtrack to choose $t_2$.

- Alternation. The strategy $t = t_1||t_2$, is the strategy that first tries to apply $t_1$ to $N$. If the result of the visit function, using the strategy $t_1$ is successful, then $t$ behaves as $t_1$. Otherwise $t = t_2$.

- Sequencing. The strategy $t = t_1; t_2$ succeeds if both $t_1$ and $t_2$ are applicable. Fails otherwise. In particular $(tN)$ is equal to $(t_2(t_1N))$.

- Star. The strategy $t^*$ behaves as the expression $\mu X. (t; X|\text{Skip})$, that is, the strategy $t$ is applied as much as is possible, and then returns the result of the computation when it fails. Intuitively, if the strategy $t$ succeeds $m$ times the result will be $t_1(t_2(...(t_mN)...))$ where each incarnation $t_i$ is $t$ itself.

The third form of non-determinism is the aforementioned choice of one rule instance (partition) of the current node from potentially many rule instances (partitions) of the current node. As we saw, the different instances are obtained by choosing different formulae as the principal formulae.

Then, this nondeterminism can be resolved by using optimisation techniques based on logic-specific considerations used to reduce the size of the search space. For example, if the chosen rule is an $(\lor)$-rule, heuristics such as MOMS [?] (Maximum number of Occurrences in disjunctions of Minimum Size) or iMOMS [?] (inverted MOMS) order the disjunctions (formulae) in the node to always choose the less/more constrained disjunct, which, in principle, should lead to an earlier clash.

3.2 Controlling Backtracking.

The search procedure is an attempt to find a “closed” tableau, so it must recover from unsuccessful branches that do not close. For rules with “implicit branching”, the best recovery action depends upon the type of non-determinism embodied in the different rule instances.

For example, the traditional $(\land)$-rule from Figure 1 is invertible in many tableau calculi: in that case, it embodies a don’t care non-determinism for formula choice since we are free to choose any conjunction from the current node as the principal formula of this rule instance. If the chosen instance does not lead to a closed denominator, then there is no need to backtrack over the other different conjunctions in the current node since invertibility guarantees that none of them will lead to a closed denominator. Operationally, it is currently not feasible to automatically detect whether a rule is invertible in a given tableau calculus, so one way to declare a rule as invertible is by writing it as $(\land_{\text{inv}})$ using a double-line separator as shown in Figure 1.
On the other hand, in the traditional \((K)\)-rule, the implicit branching is essential since different choices may give different results, thus embodying a form of don’t know non-determinism. For example, consider the different choices of principal \(\Diamond\)-formula for a node containing both \(\Diamond p\) and \(\Diamond \bot\): the \(\Diamond p\)-choice may or may not close, but the \(\Diamond \bot\)-choice is guaranteed to close. That is, if one rule instance does not close then we must backtrack over the other possible rule instances until we find an instance that gives a closed denominator or all instances are found to be open, before backtracking further.

Traditional tableau calculi do not envisage any form of communication between the branches of a tableau, but operationally we wish to allow such communication. For traditional explicitly branching rules like \((\lor)\), it is possible to add decorations that allow inter-branch communication. But this is not possible with the branches implicit in the choice of principal formula of the \((K)\) rule. We therefore allow the denominators of a rule to be separated by a new type of separator ‘||’ which captures “existentially branching”: the numerator is closed if some denominator is closed. This is dual to the “universally branching” separator ‘\(|\)’ used for explicitly branching rules like \((\lor)\): the numerator is closed if all denominators are closed.

Figure 2 shows two ways of “determinising” the implicit backtracking in the \((K)\)-rule using existential branching. By our maximality constraint on numerator patterns, the rule \((\text{det-K})\) instructs us to partition the numerator into \(n\) principal \(\Diamond\)-formulae, a container \(\Box X\) for all the \(\Box\)-formulae, and a container \(W\) for all the other formulae. The double-lines tells us to commit to this partition and the ‘\(|\)’ separator tells us that the numerator is closed if some denominator is closed. This rule is actually difficult to implement since the parameter \(n\) is effectively a free variable which must be instantiated. But we can determinise even this aspect by using a recursive version called the \((\text{rec-K})\)-rule from Figure 2 instead which can be read as: choose a principal formula \(\Diamond P\), put all other \(\Diamond\)-formulae in \(\Diamond Y\), put all \(\Box\)-formulae in \(\Box X\), put all non-boxed and non-diamond formulae in \(W\), commit to this partition, and close the numerator if some denominator closes. By repeatedly applying \((\text{rec-K})\) to the right denominator, we can step through the same partitions as the \((\text{det-K})\) rule, without having to worry about the value of \(n\) since the \((\text{rec-K})\) rule will fail to apply when the right denominator contains no \(\Diamond\)-formulae because \(\Diamond P\) cannot be empty. We need a strategy to ensure that no other rules are applied between these consecutive applications of \((\text{rec-K})\) but it is easy to capture such a strategy using the tactic language.

The traditional \((\lor)\)-rule also contains a form of implicit branching since different choices of the principal formulae may be possible if the current node contains more than one disjunction. So we also need to explicitly declare whether such rules are to be treated as invertible by using a double-line separator as for the \((\land_{\text{inv}})\)-rule.

From a general perspective, the two types of branching can be characterised as conditionally branching: “explore different denominators until some user-defined condition becomes true”, with both universal and existential branching as instances.

Our resulting rule classification is shown in Table 1. Linear rules have one denominator, while branching rules have two or more which are universal or existential related. Each rule can either commit or not commit to the partition (instantiation) selected first by the formula-choice heuristic (by being invertible or non-invertible).
Table 1

<table>
<thead>
<tr>
<th>Instance choice</th>
<th>Branching</th>
<th>Linear</th>
</tr>
</thead>
<tbody>
<tr>
<td>Backtrack</td>
<td>(\lor)</td>
<td>-</td>
</tr>
<tr>
<td>Commit</td>
<td>(\lor_{inv})</td>
<td>(rec-K)</td>
</tr>
</tbody>
</table>

If the rule commits then only this first partition is considered while expanding the denominator(s). If the rule does not commit then the denominator(s) will be re-instantiated for each partition generated by the application of the rule numerator to the current node until an instantiation is found that closes the numerator. With this rule classification it is easier to mechanize tableau rules as specified in the literature whilst removing non-determinism. Rules for classical modal logic can be characterized as shown. In Table 1 we indicate with the symbol “-” combinations that cannot be expressed in the TWB using a single rule. Nonetheless these can be expressed by using two rules “chained” in the strategy with the sequence operator.

4 Defining the Calculus for a Logic

In this section we detail the TWB syntax using as a running example a tableau calculus for S4 from [?] and we will assume familiarity with it. A logical module in the TWB is composed of three main parts: the grammar definition, the logical rules and the strategy.

4.1 Defining the grammar

The keyword CONNECTIVES in the TWB introduces a list of strings separated with a semicolon ";". Each string can be used as a connective in the grammar definition (below) and it will become a reserved keyword in the module. Connectives can be of variable length, can be composed by a mix of numbers, symbols and characters.

CONNECTIVES [ "-";"&";"v";"->";"<->";"<>";"[]" ]

The keyword GRAMMAR introduces the specification of the grammar used in the module to write formulae and rules. A TWB grammar is composed of a sequence of productions separated by a double semicolon ";;". Two mandatory productions are formula and expr. A third pre-defined production that can be omitted is node.

- node: this production defines the shape of a tableau/sequent node. By default, a tableau node is composed of a set of formulae.
- expr: this production defines the outer most expressions used in the definition of tableau rules. Generally an expression is just a formula. In more complicated tableau rules, an expression can be a formula decorated with a label or with another arbitrary data structure.
- formula : this production defines the shape of the formula definition to be used in the tableau rules.
The grammar accepted by the TWB is a loose LL(1) grammar. Conflicts are not handled automatically and the definition of ambiguous grammars can lead to unspecified results. In the grammar definition we use these three conventions: lowercase identifiers in a production are interpreted as grammar identifiers for a production; upper-case identifiers are interpreted as constants (e.g. Verum and Falsum); and the keyword ATOM identifies an anonymous atom in the grammar.

4.2 Defining histories and variables

The TWB has the infrastructure to add histories and variables to tableau/sequent rules. Histories are used to pass information top-down from numerator to denominators and are typically used to implement blocking techniques. Variables are used to pass information bottom-up from already explored sub-trees to parents. The traditional notion of a branch being “Open” or “Closed” is carried from the leaves to the root by a default variable called status.

Operationally, a history or a variable is an object that must be instantiated by the user when defining a logic module. The TWB library defines the interface for such objects in terms of an Ocaml functor. The TWB data types library defines three generic data structures that can be assembled by the user to define complex histories or variables. A functor is a function that given a module of type Element-TYPE returns a module of type TwbSet.S. The Element-TYPE type module has the following signature:

```ocaml
module type ValType =
  sig
    type t
    val copy : t -> t
    val to_string : t -> string
  end
```

The three basic functors to build such data structures are: TwbSet.Make (defines a set of elements), TwbMSet.Make (defines a multi set of elements) and Twb-List.Make (defines a list of elements). To add a history of type “set of formulae” we need to define a module FormulaSet by using the functor TwbSet.Make and pass to it the type formula as Element-TYPE as shown below.

```ocaml
module FormulaSet = TwbSet.Make(     struct
```

8
type t = formula
let to_string = formula_printer
let copy s = s
end

Once the module is defined, we add it to the tableau/sequent node using the following syntax. The keyword HISTORIES expects a sequence of history declarations. Each such declaration consists of three elements. The first element is an upper-case identifier (e.g. UBXS) naming the history used in the tableau rules, followed by a colon. The second element is the type of the history (e.g FormulaSet.Set), followed by an := operator. The third element is the default value for the history (e.g. a new empty object of type FormulaSet.set).

HISTORIES
    UBXS : FormulaSet.set := new FormulaSet.set ;
    DIAS : FormulaSet.set := new FormulaSet.set
END

Variables are declared similarly with the following syntax. The only difference is that the identifier used for variables is always lower-case.

VARIABLES
    status : String := "Closed"
END

4.3 Defining tableau rules

The collection of rules are enclosed within keywords TABLEAU and END. Rules are specified via the RULE and END keywords with principal formulae enclosed in braces.

TABLEAU

RULE Id { a } ; { ~ a } ; Z == Close END
RULE False Falsum == Close END
RULE And { A & B } == A ; B END
RULE Or { A v B } == A | B END

RULE T
{ [] P }

P
COND notin(P, UBXS)
ACTION [
    UBXS := add(P,UBXS);
    DIAS := emptyset(DIAS)
]

---

3 Is it FormulaSet.Set or FormulaSet.set?
The simplest tableau rule has a name \texttt{Id} and a numerator pattern which partitions the current node into three disjoint parts: an atom \(a\); its negation \(\sim a\); and an (unrestricted) container \(Z\). Note that atoms are specified using a lower case identifier, while sets of formulae using an upper-case identifier.

Since any such clash is sufficient to close the branch, we instruct this rule to commit to the first partition that matches by using a separator of at least two “==” symbols. The directives \texttt{Close} or \texttt{Open} or \texttt{Stop} set the value of the default variable \texttt{status}, stopping the visit procedure and triggering backtracking. Thus the \texttt{Id} rule closes the current branch. The rule \texttt{False} closes the current branch if one occurrence of constant \texttt{False} is found. For conciseness, rules can be written on one line.

The \texttt{And} rule is written to highlight that rules can capture simple rewriting. It has a single (non-empty) principal formula \(A\&B\), with \textit{no accompanying unrestricted container} like \(Z\). This is a signal to replace (rewrite) \(A\&B\) with \(A\) and \(B\) and carry all other formulae from the numerator into the denominator. A more traditional way to write this rule would use \(Z\) (say) in both the numerator and the denominator.

The \texttt{Or} rule also uses rewriting but uses universal branching to create a left child containing \(A\) and a right child containing \(B\).

The \texttt{T} rule rewrites \(\Box P\) to \(P\) but only if the side-condition declared using the \texttt{COND} construct is true. This condition checks whether \(P \notin UBXS\) using a function \texttt{notin(.)}. Its \texttt{ACTION} directive constructs the histories of its child by adding \(P\) to the current history \texttt{UBXS} and setting the history \texttt{DIAS} to be the empty set (because it has seen a \(\Box\)-formula new to \texttt{DIAS} as explained in [?]).

The \texttt{S4} rule chooses a principal formula \(\Diamond P\) from the numerator and creates a child containing both \(P\) and the set contained in the history \texttt{UBXS} but only if the side-condition \(\Diamond P \notin DIAS\) specified via \texttt{COND} is true. Its \texttt{ACTION} directive constructs its child’s history \texttt{DIAS} by adding \(\Diamond P\) to the current history \texttt{DIAS} but leaves \texttt{UBXS} intact. It does not commit to the choice of principal formula since it uses a separator consisting of at least two “==” symbols, which means that if this child does not close, then this rule will backtrack over the different principal \(\Diamond\)-formula choices. The same rule can also being specified by making the backtracking explicit as follows:

\begin{verbatim}
RULE S4H
{ <> P } ; <> Y ; Z
---------------------
A ; UBXS || <> Y
\end{verbatim}
COND notin(<> P, DIAS)
ACTION [ [ DIAS := add(<> A,DIAS)] ; [ ] ]
END

The body of the rule is composed of a principal formula, a possibly empty set of diamond formulae ⋄ Y and an anonymous set Z. Note that now because of the presence of the schema ⋄ Y, the set Z is diamond-formula free. The denominator has two branches: A;UBXS encodes the modal jump while ⋄ Y encodes a recursion step to consider all other diamonds if the first branch does not close.

Note also that we now use the double line “==” as the rule has been determinised and no backtracking is needed to recover from a wrong choice. Moreover the double bar “||” set an existential branching which closes the numerator if some denominator closes. Thus, the second branch is explored if and only if the result of the tableau rooted with the node A;UBXS is open. The functions to manipulate histories and side conditions are explained below.

4.3.1 Auxiliary Functions
In the TWB we can use arbitrary OCaml functions. In our example we use three functions to handle histories defined as follows:

let add (l,h) = h#addlist l
let notin (l,h) = not(h#mem (List.hd l))
let emptyset h = h#empty

• add(formula list, history): accepts a list of formulae and a history object and returns the history object with the formula list added to it.
• notin(formula list, history): accepts a list of formulae and a history, and returns a boolean indicating if the list of formulae is in the history.
• emptyset(history): returns an empty history object.

4.4 Defining the Strategy

The strategy specifies the order in which rules are applied during proof search. In our example, for completeness, we need to apply all classical rules first and then the S4-rule. The bang ! operator applies the first rule that is applicable. The star * iterates until no rule is applicable. Since the S4 rule is the last rule, this means that all the other rules are not applicable. In other words, the strategy says “repeatedly apply the first applicable rule from the left until none are applicable, and then apply the S4 rule, and repeat this process until no rules are applicable”. This strategy is applied to every branch of the proof tree according to the visit algorithm.

STRATEGY :=
let sat = tactic ( (False ! Id ! And ! T ! Or) )
in tactic ( (sat ! S4 )* )
5 Conclusion and further work

In this paper we presented a new version of the Tableau WorkBench. Both the architecture and the user interface have been substantially changed from the previous version presented at TABLEAU 2003. An intermediate version of the TWB can be found in [?] where we also presented an array of benchmarks that compare the TWB with the LWB[?] showing that the TWB can compete with the LWB only if well known optimisations (such as simplification or back-jumping) are incorporated in the tableau calculus. As further work, we are working to re-implement such optimisations with the new version and to reproduce up-to-date benchmarks. The TWB can be downloaded from the website http://twb.rsise.anu.edu.au